Catz, Ratz, and Batz Game Rules

In the Catz, Ratz, and Batz game (which can be purchased on-line or in game stores) there are nine 6-sided dice. Each die has a 3, a 5, a 7, a cat, a bat, and a rat. To start a turn, each player rolls all the dice. All of the animals are placed to the side. If the remaining numbers match or if there are no numbers, the turn is over. If the numbers do not match, the player chooses to keep one kind of number (all of the 3s, for example), and re-rolls the dice showing other numbers. The player may change the number being kept at any time until only one number remains.

After the player’s turn is over, the dice are scored. First, the numbers are added together to obtain a base score. The animals impact the base score in a slightly complicated way. Cats are always considered “good” and rats are always considered “bad”. Bats are “good” if the selected number is a 3, they are “neutral” if the selected number is a 5, and they are “bad” if the selected number is a 7. If the number of good animals is smaller than the number of bad animals, the player receives a score of zero for that turn. If the number of good animals is equal to the number of bad animals, the player receives the base score. If the number of good animals is greater than the number of bad animals, the number of bad animals is subtracted from the number of good animals (you must sacrifice a good animal to cancel out each bad animal). Each remaining good animal adds another copy of the base score to the total.

Here are some example scores:

- Cat, Cat, Cat, Bat, Rat, 5, 5, 5, 5. Base score: 20. Number of good animals: 3. Number of bad animals: 1. (The bat is neutral so it does not count.) Number of good animals remaining: 2. This means that two copies of the base score will be added to the base score for a total of 60.

- Cat, Cat, Bat, Rat, 3, 3, 3, 3, 3. Base score: 15. Number of good animals: 3. Number of bad animals: 2. Total score: 45.


- Cat, Cat, Cat, Cat, Bat, 7, 7, 7, 7. Base score: 28. Number of good animals: 4. Number of bad animals: 1. Number of good animals remaining: 3. Total score: 112.

Players take a pre-determined number of turns or play for a certain amount of time and then total their scores.

Catz, Ratz, and Batz Game Analysis

Play the Catz, Ratz, and Batz game several times so that everyone understands the scoring system. Then consider the questions below.

What is the Highest Possible Score?

To tackle this question, imagine that you could choose the outcomes of the dice rather than rolling them. You might choose some animals and some numbers. What would be the best animal to choose and what would be the best number to choose?

Make a table showing every possible combination of Cats and 7s that could be made with the dice. Make a third column on the table showing the corresponding total scores for each case.
On a coordinate grid, plot the number of Cats along the $x$-axis and the total score along the $y$-axis. What kind of graph emerges?

Create a formula that gives the total score as a function of the number of Cats. Is this function linear, quadratic, polynomial, exponential, rational, or does it have another form? Why do you think the total score function has that form?

**How Much Do Rats Lower Your Potential Score?**

Suppose that one of the dice shows a Rat. What is the highest score that is possible if you could select the remaining dice rather than rolling them? What if there are two Rats? Three Rats? Four Rats? Five or more Rats?

**What is the Probability That Your Turn Will Only Last One More Roll?**

Suppose that you have the following dice in the middle of your turn:

Cat, Bat, Bat, Bat, Bat, Rat, 3, 5, 5.

Suppose that you choose to keep the 3. What is the probability that your next roll is your last roll? In other words, what is the probability that re-rolling the two fives will result in either an animal or a 3 on each die?

**What is the Best Bet?**

Suppose that you have the following dice in the middle of your turn:

Cat, Cat, Cat, Bat, Bat, Rat, 3, 5, 7.

What are all of the possible score outcomes for your turn if you choose 3s and stick with that choice until the end? What is the probability of each of those outcomes? What is the expected value of the outcome in the case where you choose 3s?

What are all of the possible score outcomes for your turn if you choose 5s and stick with that choice until the end? What is the probability of each of those outcomes? What is the expected value of the outcome in the case where you choose 5s?

What are all of the possible score outcomes for your turn if you choose 7s and stick with that choice until the end? What is the probability of each of those outcomes? What is the expected value of the outcome in the case where you choose 7s?

Which number would be the best bet?

**Another Scenario**

Suppose that you have the following dice in the middle of your turn:

Cat, Cat, Cat, Cat, Bat, Bat, 3, 5, 7.
What are all of the possible score outcomes for your turn if you choose 3s and stick with that choice until the end? What is the probability of each of those outcomes? What is the expected value of the outcome in the case where you choose 3s?

What are all of the possible score outcomes for your turn if you choose 5s and stick with that choice until the end? What is the probability of each of those outcomes? What is the expected value of the outcome in the case where you choose 5s?

What are all of the possible score outcomes for your turn if you choose 7s and stick with that choice until the end? What is the probability of each of those outcomes? What is the expected value of the outcome in the case where you choose 7s?

Which number would be the best bet?

**Analyze Your Own Scenario**

Make up your own scenario and analyze the expected values for various choices.
Catz, Ratz, and Batz Game: Lesson Plan

Students learn to play a dice game called Catz, Ratz, and Batz. Analysis of the game reveals a quadratic function that governs the maximum possible score on each turn. Students also consider questions of expected value corresponding to various choices in the game to determine what is the best option.

Levels 7th through 12th grade

Topics Multiplication facts, Quadratic functions, Modeling, Probability, Expected value

Goals

- Students will explore a scenario that can be modeled by a quadratic function.
- Students will compute expected values to discover the best strategy for certain situations in a game.

Pre-requisite Knowledge Multiplication facts, Familiarity with quadratic functions, Familiarity with expected value and probability concepts.

Preparation Time 5 minutes.

Activity Time 60 to 120 minutes.

Materials and Preparation

- Notebook paper
- Graph paper
- Pencils
- Catz, Ratz, and Batz games for groups to play.

Author Amanda Katharine Serenevy

Sources

Helpful Hints for Activity Leaders

What is the Highest Possible Score?

To obtain the highest score in the Catz, Ratz, and Batz game, it would be best to have some combination of Cats and 7s on the nine dice. The table below shows all of these combinations:

<table>
<thead>
<tr>
<th>Cats</th>
<th>7s</th>
<th>Total Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>9</td>
<td>63</td>
</tr>
<tr>
<td>1</td>
<td>8</td>
<td>112</td>
</tr>
<tr>
<td>2</td>
<td>7</td>
<td>147</td>
</tr>
<tr>
<td>3</td>
<td>6</td>
<td>168</td>
</tr>
<tr>
<td>4</td>
<td>5</td>
<td>175</td>
</tr>
<tr>
<td>5</td>
<td>4</td>
<td>168</td>
</tr>
<tr>
<td>6</td>
<td>3</td>
<td>147</td>
</tr>
<tr>
<td>7</td>
<td>2</td>
<td>112</td>
</tr>
<tr>
<td>8</td>
<td>1</td>
<td>63</td>
</tr>
<tr>
<td>9</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

From the table, it is clear that the best score occurs when there are four Cats and five 7s. In this case, the base score would be $7 \cdot 5 = 35$. The four cats would add four additional copies of this score to the base score – in other words, they effectively multiply the score by 5. The total score is then $35 \cdot 5 = 175$.

Graphing the Points

If we plot the points from the table, we see that the values lie along a curve that looks as though it might be a parabola.
Formula for the Total Score as a function of the Number of Cats

Let $C$ stand for the number of Cats. Then $9 - C$ stands for the number of 7s. The base score will be obtained by multiplying the number of 7s by seven. So the base score is $7(9 - C)$. This base score will be multiplied by one more than the number of Cats to obtain the total score. Therefore the total score is given by the following formula:

$$\text{Total Score} = 7(9 - C)(C + 1) = -7C^2 + 56C + 63$$

We can see that this is a quadratic function which confirms that the points we plotted in the last section do indeed lie along a parabola. The vertex of this parabola is at $(4, 175)$ which corresponds to the maximum possible score for a turn of Catz, Ratz, and Batz.

The reason that this function turns out to be a quadratic function is that the base score and the multiplier are competing for how many dice are allocated for each purpose. The largest product is obtained when these two values are identical. When one is larger and the other is smaller, the result is not as large. This is reminiscent of problems where the area of a rectangle is maximized while the sum of the length and width is fixed.

How Much do Rats Lower Your Potential Score?

Suppose that one of the dice shows a Rat, but we are allowed to select the other dice so that the score is as large as possible. At least one Cat must be allocated to cancel out the Rat. The remaining seven dice can be chosen to be whichever combination of Cats and 7s gives the largest score. The formula for the total score would then be If $C$ stands for the number of cats on the remaining seven dice (not counting the one needed to cancel the rat), then the formula for the total score is:

$$\text{Total Score} = 7(7 - C)(C + 1) = -7C^2 + 42C + 49$$

This parabola has its maximum at the vertex at $(3, 112)$

In general, each additional mandated Rat reduces the number of dice that count towards the total score by two. Thus, if $R$ is equal to the number of mandated Rats, the Total Score is given by

$$\text{Total Score} = 7(9 - 2R - C)(C + 1) = -7C^2 + (56 - 14R)C + (63 - 14R)$$

The vertex of this parabola is located at $(4 - R, 7(5 - R)^2)$. If there are 5 or more Rats, there cannot be enough Cats to counteract the Rats and so the score would be 0. Here is a table showing how the number of Rats impacts the maximum possible score:
<table>
<thead>
<tr>
<th>Rats</th>
<th>Maximum Possible Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>175</td>
</tr>
<tr>
<td>1</td>
<td>112</td>
</tr>
<tr>
<td>2</td>
<td>63</td>
</tr>
<tr>
<td>3</td>
<td>28</td>
</tr>
<tr>
<td>4</td>
<td>7</td>
</tr>
<tr>
<td>5 or more</td>
<td>0</td>
</tr>
</tbody>
</table>

**What is the Probability That Your Turn Will Only Last One More Roll?**

We are supposing that you have the following dice showing in the middle of your turn, and that we are keeping the 3.

Cat, Bat, Bat, Bat, Bat, Rat, 3, 5, 5.

What is the probability that re-rolling the two fives will result in either an animal or a 3 on each die?

Each die has a \( \frac{4}{6} = \frac{2}{3} \) probability of rolling either an animal or a 3. Since the outcomes of the two dice are independent of one another, we can obtain the overall probability by multiplying the two probabilities. Therefore, the overall probability that the turn will only last one more roll is \( \frac{2}{3} \cdot \frac{2}{3} = \frac{4}{9} \). That means the probability is slightly greater than one half that your turn will not end with one more roll.

**What is the Best Bet?**

We are supposing that you have the following dice in the middle of your turn:

Cat, Cat, Cat, Bat, Bat, Rat, 3, 5, 7

**Expected Value if You Choose 3 and Stick With That Choice**

If the dice showing the 5 and 7 are re-rolled and show either a 5 or 7, it is as if they were not rolled at all since we will not keep those values. Each die has four possibilities for how it could end up. The 16 overall possible outcomes are listed below along with the corresponding total scores. (Remember that Bats count as good animals with 3s.)

- Cat, Cat, Cat, Bat, Bat, Rat, 3, Cat, Cat – Total Score: 21
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Cat, Bat – Total Score: 21
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Cat, Rat – Total Score: 15
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Cat, 3 – Total Score: 36
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Bat, Cat – Total Score: 21
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Bat, Bat – Total Score: 21
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Bat, Rat – Total Score: 15
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Bat, 3 – Total Score: 36
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Rat, Cat – Total Score: 15
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Rat, Bat – Total Score: 15
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Rat, Rat – Total Score: 9
- Cat, Cat, Cat, Bat, Bat, Rat, 3, Rat, 3 – Total Score: 24
- Cat, Cat, Cat, Bat, Bat, Rat, 3, 3, Cat – Total Score: 36
We can condense this list as follows:

<table>
<thead>
<tr>
<th>Score</th>
<th>Probability</th>
<th>Score × Probability</th>
</tr>
</thead>
<tbody>
<tr>
<td>45</td>
<td>$\frac{1}{16}$</td>
<td>$\frac{45}{16}$</td>
</tr>
<tr>
<td>36</td>
<td>$\frac{4}{16}$</td>
<td>$\frac{144}{16}$</td>
</tr>
<tr>
<td>24</td>
<td>$\frac{2}{16}$</td>
<td>$\frac{48}{16}$</td>
</tr>
<tr>
<td>21</td>
<td>$\frac{4}{16}$</td>
<td>$\frac{84}{16}$</td>
</tr>
<tr>
<td>15</td>
<td>$\frac{4}{16}$</td>
<td>$\frac{60}{16}$</td>
</tr>
<tr>
<td>9</td>
<td>$\frac{1}{16}$</td>
<td>$\frac{9}{16}$</td>
</tr>
</tbody>
</table>

Expected Value | 24.375

We could have obtained the same number by simply taking the average of the 16 possible scores. Either way we calculate this, we see that choosing a 3 results in an expected score of 24.375.

**Expected Value if You Choose 5 and Stick With That Choice**

If the dice showing the 3 and 7 are re-rolled, each die has four possibilities for how it could end up. The 16 overall possible outcomes are listed below along with the corresponding total scores. (Remember that Bats are neutral with 5s.)

- Cat, Cat, Cat, Bat, Bat, Rat, Cat, 5, Cat – Total Score: 25
- Cat, Cat, Cat, Bat, Bat, Rat, Cat, 5, Bat – Total Score: 20
- Cat, Cat, Cat, Bat, Bat, Rat, Cat, 5, Rat – Total Score: 15
- Cat, Cat, Cat, Bat, Bat, Rat, Cat, 5, 5 – Total Score: 40
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, 5, Cat – Total Score: 20
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, 5, Bat – Total Score: 15
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, 5, Rat – Total Score: 10
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, 5, 5 – Total Score: 30
- Cat, Cat, Cat, Bat, Bat, Rat, Rat, 5, Cat – Total Score: 15
- Cat, Cat, Cat, Bat, Bat, Rat, Rat, 5, Bat – Total Score: 10
- Cat, Cat, Cat, Bat, Bat, Rat, Rat, 5, Rat – Total Score: 5
- Cat, Cat, Cat, Bat, Bat, Rat, Rat, 5, 5 – Total Score: 20
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, 5, 5, Cat – Total Score: 40
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, 5, 5, Bat – Total Score: 30
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, 5, 5, Rat – Total Score: 20
- Cat, Cat, Cat, Bat, Bat, Rat, 5, 5, 5 – Total Score: 45

We can condense this list as follows:
<table>
<thead>
<tr>
<th>Score</th>
<th>Probability</th>
<th>Score × Probability</th>
</tr>
</thead>
<tbody>
<tr>
<td>45</td>
<td>1/15</td>
<td>45/15</td>
</tr>
<tr>
<td>40</td>
<td>2/15</td>
<td>80/15</td>
</tr>
<tr>
<td>30</td>
<td>2/15</td>
<td>60/15</td>
</tr>
<tr>
<td>25</td>
<td>1/15</td>
<td>25/15</td>
</tr>
<tr>
<td>20</td>
<td>4/15</td>
<td>80/15</td>
</tr>
<tr>
<td>15</td>
<td>3/15</td>
<td>45/15</td>
</tr>
<tr>
<td>10</td>
<td>2/15</td>
<td>20/15</td>
</tr>
<tr>
<td>5</td>
<td>1/15</td>
<td>5/15</td>
</tr>
<tr>
<td></td>
<td></td>
<td><strong>Expected Value</strong> 22.5</td>
</tr>
</tbody>
</table>

We can see that choosing a 5 results in an expected score of 22.5.

**Expected Value if You Choose 7 and Stick With That Choice**

If the dice showing the 3 and 5 are re-rolled, each die has four possibilities for how it could end up. The 16 overall possible outcomes are listed below along with the corresponding total scores. (Remember that Bats are bad animals like Rats with 7s.)

- Cat, Cat, Cat, Bat, Bat, Bat, Cat, Cat, 7 – Total Score: 21
- Cat, Cat, Cat, Bat, Bat, Bat, Rat, Cat, Cat, 7 – Total Score: 7
- Cat, Cat, Cat, Bat, Bat, Rat, Cat, Bat, Cat, 7 – Total Score: 7
- Cat, Cat, Cat, Bat, Bat, Rat, Cat, Bat, Rat, Cat, 7 – Total Score: 28
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Cat, 7 – Total Score: 7
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Rat, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Rat, Bat, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Rat, Bat, Bat, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Rat, Bat, Bat, Rat, 7 – Total Score: 28
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7, 7 – Total Score: 28
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7, 7 – Total Score: 0
- Cat, Cat, Cat, Bat, Bat, Rat, Bat, Bat, Bat, 7, 7 – Total Score: 21

We can condense this list as follows:
We can see that choosing a 7 results in an expected score of 7.875.

The Best Option

When you have already rolled the following dice
Cat, Cat, Cat, Bat, Bat, Rat, 3, 5, 7

the best choice is to save the 3 and re-roll the 5 and the 7.

Another Scenario

This time we are supposing that you have the following dice in the middle of your turn:
Cat, Cat, Cat, Bat, Bat, 3, 5, 7.

If you save the 3 and re-roll the 5 and 7, the 16 possible outcomes are:

- Cat, Cat, Cat, Cat, Bat, Bat, 3, Cat, Cat – Total Score: 27
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Cat, Bat – Total Score: 27
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Cat, Rat – Total Score: 21
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Cat, 3 – Total Score: 48
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Bat, Cat – Total Score: 27
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Bat, Bat – Total Score: 27
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Bat, Rat – Total Score: 21
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Bat, 3 – Total Score: 48
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Rat, Cat – Total Score: 21
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Rat, Bat – Total Score: 21
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Rat, Rat – Total Score: 15
- Cat, Cat, Cat, Cat, Bat, Bat, 3, Rat, 3 – Total Score: 36
- Cat, Cat, Cat, Cat, Bat, Bat, 3, 3, Cat – Total Score: 48
- Cat, Cat, Cat, Cat, Bat, Bat, 3, 3, Bat – Total Score: 48
- Cat, Cat, Cat, Cat, Bat, Bat, 3, 3, Rat – Total Score: 30
- Cat, Cat, Cat, Cat, Bat, Bat, 3, 3, 3 – Total Score: 63

The expected value of the score if you choose to save the 3 is 33.

If you save the 5 and re-roll the 3 and 7, the 16 possible outcomes are:

- Cat, Cat, Cat, Cat, Bat, Bat, Cat, 5, Cat – Total Score: 35
- Cat, Cat, Cat, Cat, Bat, Bat, Cat, 5, Bat – Total Score: 30
• Cat, Cat, Cat, Cat, Bat, Bat, Cat, 5, Rat – Total Score: 25
• Cat, Cat, Cat, Cat, Bat, Bat, Bat, 5, Rat – Total Score: 20
• Cat, Cat, Cat, Cat, Bat, Bat, Bat, 5, Bat – Total Score: 25
• Cat, Cat, Cat, Cat, Bat, Bat, Bat, 5, 5 – Total Score: 50
• Cat, Cat, Cat, Cat, Bat, Bat, Rat, 5, Cat { Total Score: 25
• Cat, Cat, Cat, Cat, Bat, Bat, Rat, 5, Bat { Total Score: 20
• Cat, Cat, Cat, Cat, Bat, Bat, Rat, 5, Rat { Total Score: 15
• Cat, Cat, Cat, Cat, Bat, Bat, Rat, 5, 5 { Total Score: 40
• Cat, Cat, Cat, Cat, Bat, Bat, 5, Cat, 5 { Total Score: 60
• Cat, Cat, Cat, Cat, Bat, Bat, 5, Bat, 5 { Total Score: 50
• Cat, Cat, Cat, Cat, Bat, Bat, 5, Rat, 5 { Total Score: 40
• Cat, Cat, Cat, Cat, Bat, Bat, 5, 5, 5 { Total Score: 75

The expected value of the score if you choose to save the 5 is 37.5.

If you save the 7 and re-roll the 3 and 5, the 16 possible outcomes are:

• Cat, Cat, Cat, Cat, Bat, Bat, Cat, Cat, 7 { Total Score: 35
• Cat, Cat, Cat, Cat, Bat, Bat, Cat, Bat, 7 { Total Score: 21
• Cat, Cat, Cat, Cat, Bat, Bat, Cat, Rat, 7 { Total Score: 21
• Cat, Cat, Cat, Cat, Bat, Bat, Cat, 7, 7 { Total Score: 56
• Cat, Cat, Cat, Cat, Bat, Bat, Bat, Bat, 7 { Total Score: 7
• Cat, Cat, Cat, Cat, Bat, Bat, Bat, Rat, 7 { Total Score: 7
• Cat, Cat, Cat, Cat, Bat, Bat, Bat, 7, 7 { Total Score: 28
• Cat, Cat, Cat, Cat, Bat, Bat, Rat, Cat, 7 { Total Score: 21
• Cat, Cat, Cat, Cat, Bat, Bat, Rat, Bat, 7 { Total Score: 7
• Cat, Cat, Cat, Cat, Bat, Bat, Rat, Rat, 7 { Total Score: 7
• Cat, Cat, Cat, Cat, Bat, Bat, 7, Cat, 7 { Total Score: 56
• Cat, Cat, Cat, Cat, Bat, Bat, 7, Bat, 7 { Total Score: 28
• Cat, Cat, Cat, Cat, Bat, Bat, 7, Rat, 7 { Total Score: 28
• Cat, Cat, Cat, Cat, Bat, Bat, 7, 7, 7 { Total Score: 63

The expected value of the score if you choose to save the 7 is 27.125.

So for this scenario the best option is to save the 5 and re-roll the 3 and the 7.