

# CHINESE ROD NUMERAL MULTIPLICATION

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Counting rods and rod numerals are attested to throughout eastern Asia from the 5<sup>th</sup> century BCE.



Calculations done on a counting board using methods similar to (multiplication) or the same as (division) Western algorithms



# Base 10 place-value system

\*ingenious way to depict place value without zero

Positive numbers

	0	1	2	3	4	5	6	7	8	9
Vertical							┐	└┐	└└┐	└└└┐
Horizontal		—	==	≡	≡≡	≡≡≡	┘	┘┘	┘┘┘	┘┘┘┘

Negative numbers

	0	-1	-2	-3	-4	-5	-6	-7	-8	-9
Vertical							┐	└┐	└└┐	└└└┐
Horizontal		—	==	≡	≡≡	≡≡≡	┘	┘┘	┘┘┘	┘┘┘┘

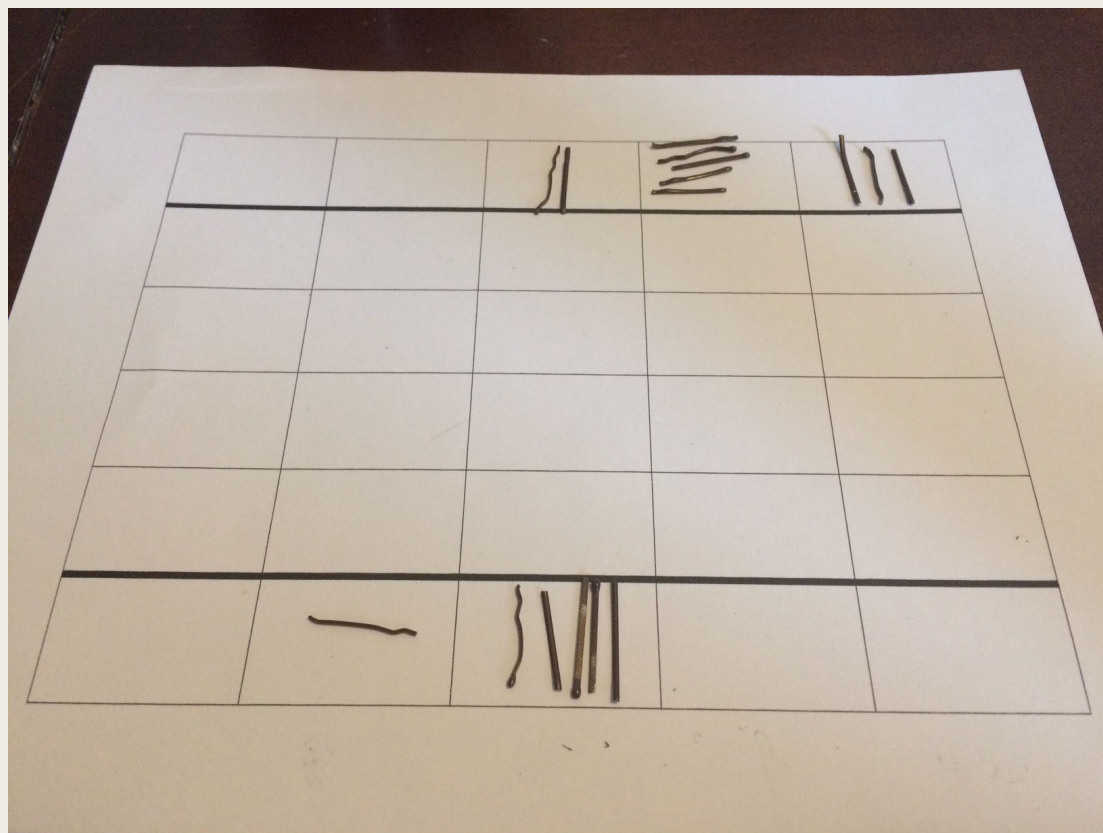
Examples:

231			≡	
5089	≡≡≡		┘	└└└┐
-407				└└┐
-6720	┘	└┐	==	

\*Alignment alternates, starting with vertical in ones digit

# Multiplication

Starts with the leading digit of the multiplicand  
as opposed to the last digit of the multiplier

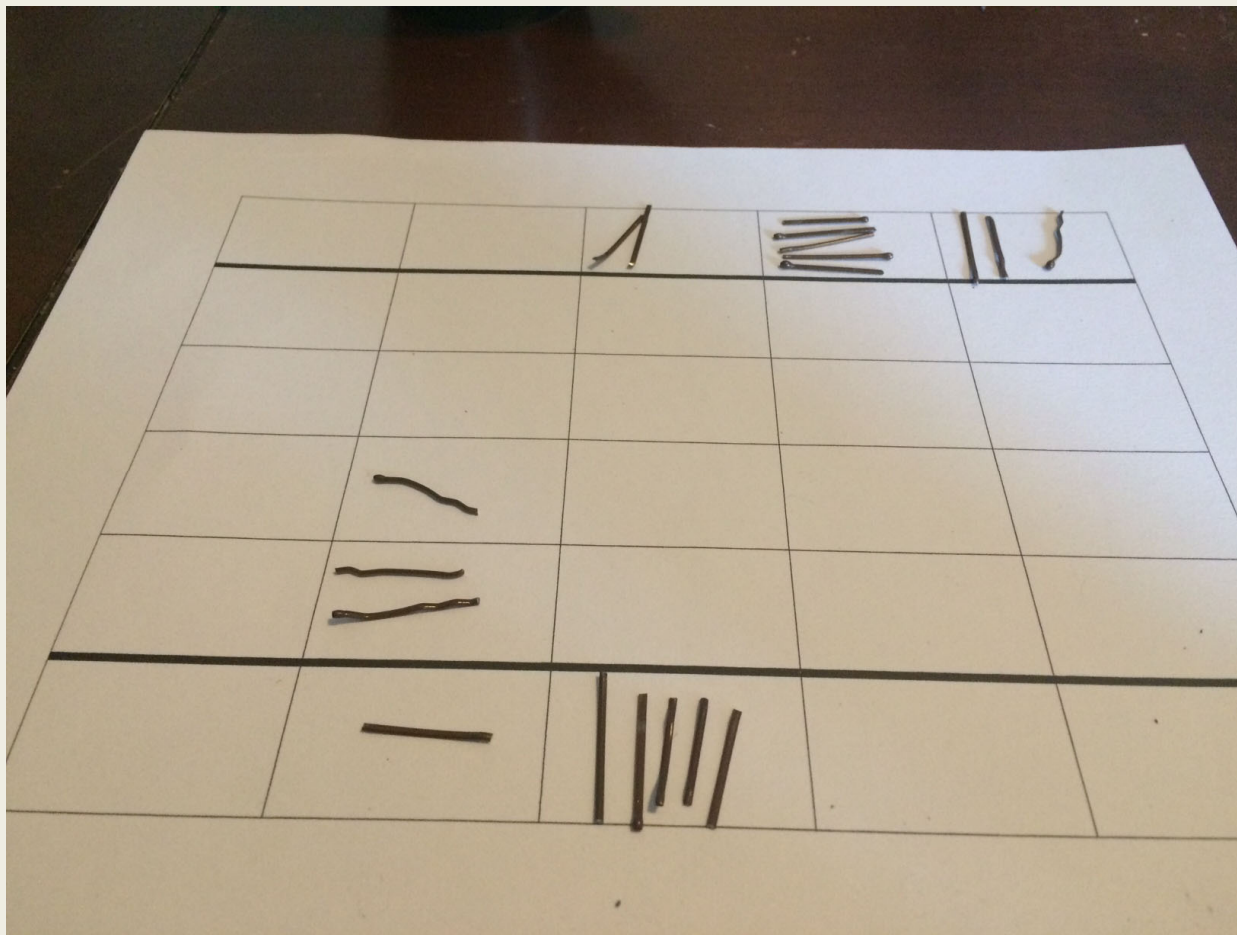


Set up

$$253 \times 15$$

Notice alignment of  
multiplier under leading  
digit of multiplicand

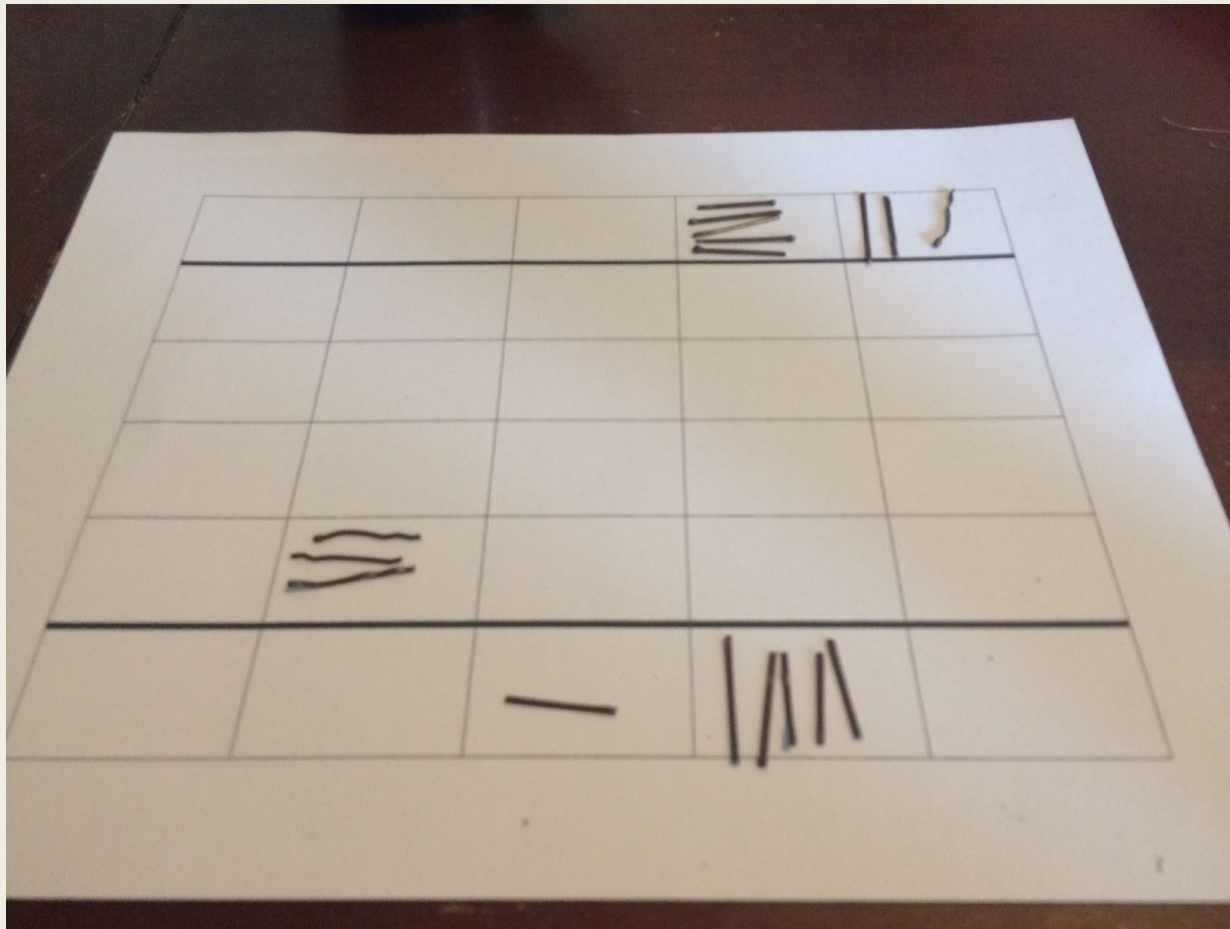
Student work using bobby pins! (they don't roll)



1<sup>st</sup> multiplication

$$2 \times 15 = 20 + 10$$

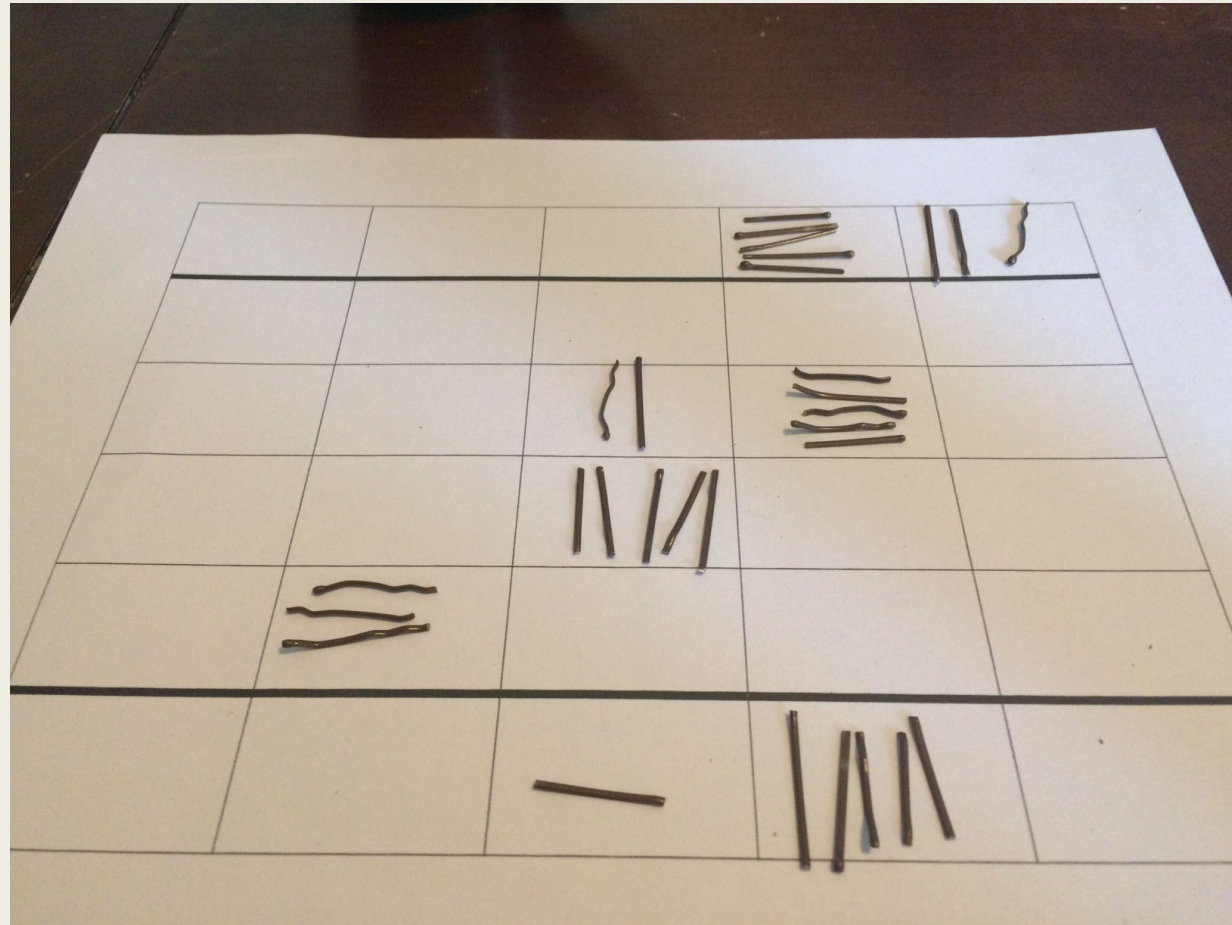
*Notice placement of multiplier's ones digit dictates placement of first partial product*



Regroup

Move multiplier one  
place to right

Remove used leading  
digit in multiplicand  
(I like this strategy!)

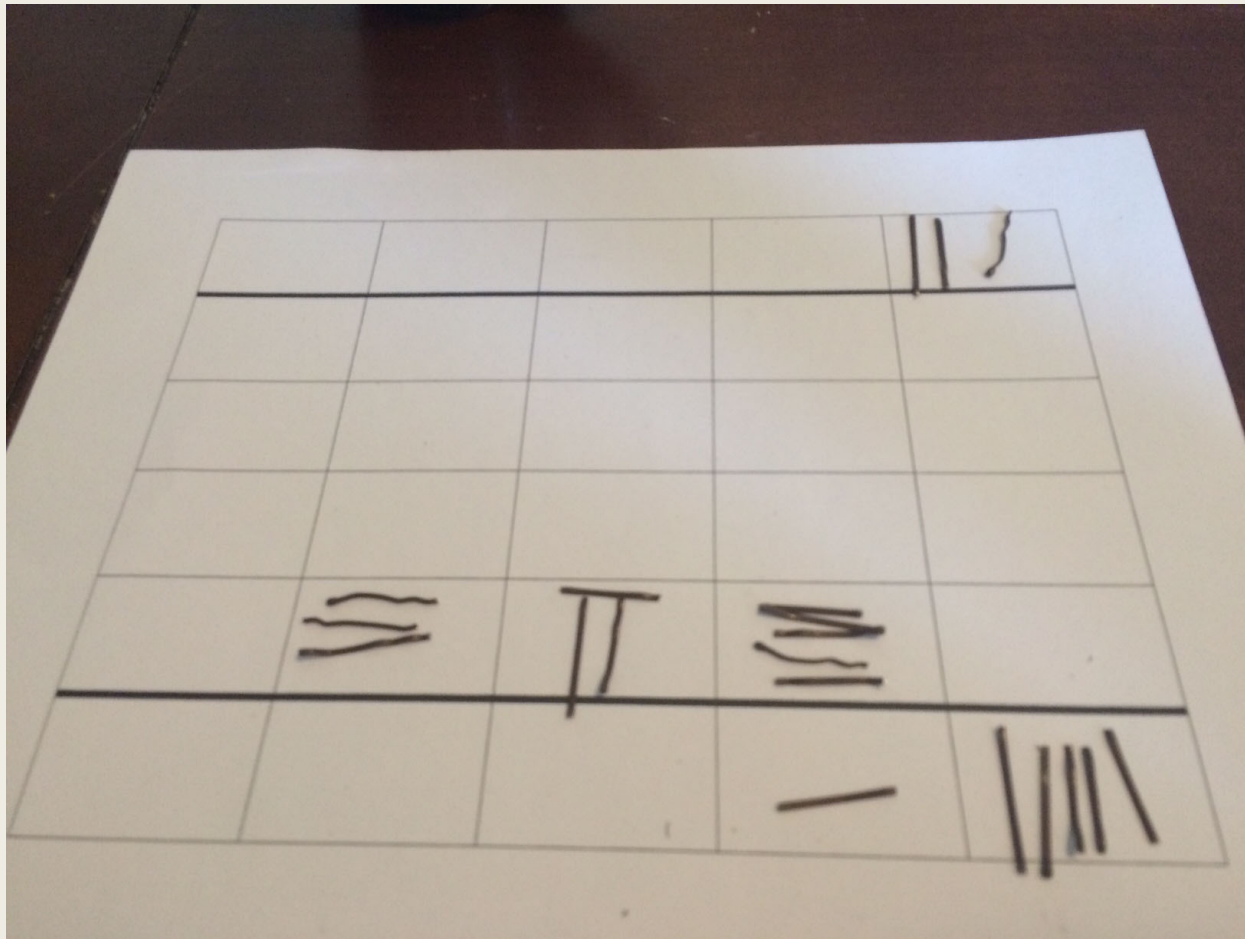


2<sup>nd</sup> multiplication

$$5 \times 15 = 50 + 25$$

*Notice bottom working row is reserved for the partial products*

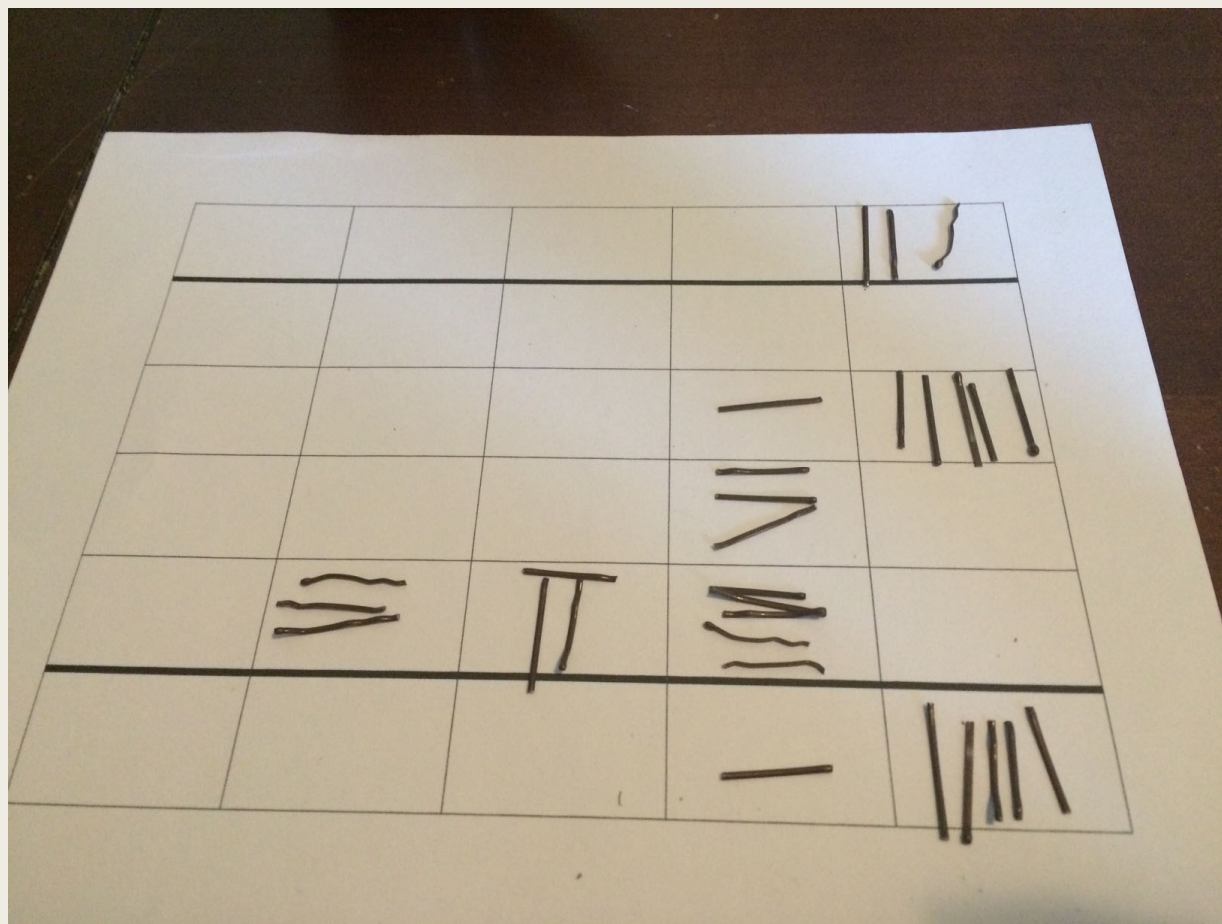




Regroup

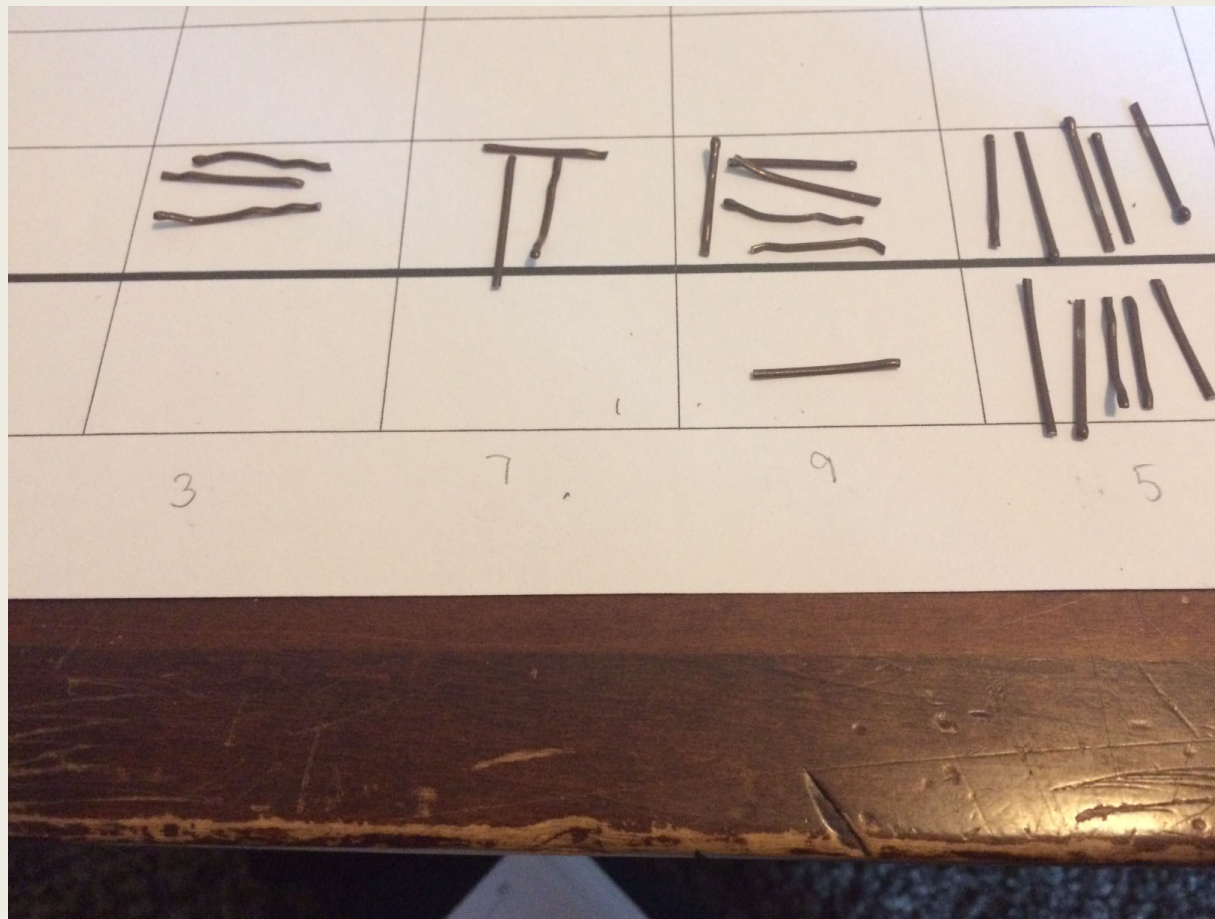
Move multiplier one  
place to right

Remove used leading  
digit in multiplicand



3<sup>rd</sup> multiplication

$$3 \times 15 = 30 + 15$$



Regroup to show final product

Remove last digit of multiplicand to indicate you are done!  
(not shown)

$$253 \times 15 = 3795$$

# Division: same as our method

Chinese Rob Numeral Division

$$2823 \div 12$$

	=	III	=	III
-	-	II		

set up

dividend

divisor

		II	III	
		IIII	=	III
		-	II	

$$42 \div 12 = 3 R 6$$



		II		
	=	IIII	=	III
	-	II		

$$26 \div 12 = 2 R 2$$



		II	III	
			-	III
			-	II

regroup & move divisor



		II	-	
		IIII	=	III
		-	II	

regroup & move divisor



		II	III	IIII
				III
			-	III

Quotient

$$63 \div 12 = 5 R 3$$

regroup remainder

$$2823 \div 12 = 235 R 3$$

Thank you very much

Famous "Pascal's" triangle by Yang Hui, 1303

